Self-dual Einstein ACH metric and CR GJMS operators in dimension three

Taiji Marugame

Academia Sinica E-mail: marugame@gate.sinica.edu.tw

Abstract

Let M be a three dimensional strictly pseudoconvex CR manifold. By refining Matsumoto's construction, we construct a one parameter family of ACH metrics g_{IJ}^{λ} ($\lambda \in \mathbb{R}$) on $M \times [0, \infty)$, which solve the Einstein equation to infinite order. When $\lambda = 0$, the metric g_{IJ}^{0} is also self-dual to infinite order. As an application, we give another proof of the fact that a three dimensional CR manifold admits CR invariant powers of the sublaplacian of all orders, which was shown by Gover–Graham.